This chapter test correlates with:

Calculus of a Single Variable, 8th ed. by Larson, Hostetler, Edwards or Houghton Mifflin, 2006 Calculus with Analytic Geometry, 8th ed. by Larson, Hostetler, Edwards Houghton Mifflin, 2006

Chapter 4: Integration

 $\begin{bmatrix} Also: \\ 7^{th} edition, Sections 4.1-4.6 \\ 6^{th} edition, Sections 4.1-4.6 \end{bmatrix}$

A few notes:

- If you are using a different textbook, this may not be a comprehensive chapter test for you.
- Solutions are available at <u>www.mathprotutoring.com/tests</u>.
- Angle measures are represented using radian measure, unless there is a pressing reason to use degree measure. If degree measure is used, there will always be a ° symbol.
- This test is copyright material. You must obtain express written permission from Linda Sinclair (<u>linda@mathprotutoring.com</u>) in order to duplicate and/or share this test with others.
- Please check <u>www.mathprotutoring.com/tests</u> soon for new tests. New ones will be added just as quickly as they are created.

Calculus Ch. 4 Integration

Questions 1-6: Find the indefinite integral.

$$1. \qquad \int (3-4t^3)dt$$

$$2. \qquad \int \frac{5x^6 - 2x}{\sqrt{x}} dx$$

3.
$$\int (3\sec^2 x + \sec 2x \tan 2x) dx$$

$$4. \qquad \int \frac{x^2}{\sqrt[4]{3x^3+5}} dx$$

5.
$$\int \frac{1-\sin^2 y}{\cos^2 y} dy$$

$$6. \qquad \int x\sqrt{x+1} \ dx$$

© 2008 Linda Sinclair. All rights reserved.

7. $\frac{dy}{dx} = (5x+2)^2$ and y passes through the point (0,1). Find the equation for y.

8. Solve the differential equation: $f''(x) = \cos x$ f'(0) = 2f(0) = 4

- 9. A rock is thrown downward with an initial velocity of 10 ft/sec from a balcony 90 ft high.
 - a. Find the rock's position function.

b. Find the amount of time it takes for the rock to hit the ground.

c. Find the rock's velocity at impact.

10. Use the upper sum with n = 4 to approximate the area between the graph of $f(x) = \frac{1}{2}x^2$ and the x-axis from x = 2 to x = 4.

11. Use the limit process to find the exact area in Question 8.

Questions 12-14: Evaluate the definite integral.

12.
$$\int_{-3}^{5} (3x^2 + 4x + 1)dx$$

$$13. \quad \int_{-3}^{2} |x-1| dx$$

$$14. \quad \int_{-\pi/2}^{\pi/2} \cos(2x) dx$$

15. If
$$\int_{1}^{3} f(x)dx = 5$$
 and $\int_{0}^{3} f(x)dx = -6$, find the value of $\int_{0}^{1} f(x)dx$.

16. Find the area between the graph of $f(x) = -\sqrt{x+3}$ and the *x*-axis, from x = 0 to x = 2.

17. If
$$f(x) = \int_{3}^{x} \sqrt{1 - \sin t} \, dt$$
, find $f'(x)$.

18. Use the Trapezoidal Rule with n = 4 to estimate the value of $\int_{-1}^{3} (2x^2 + 1) dx$.

19. Use Simpson's Rule with n = 4 to estimate the value of $\int_{-1}^{3} (2x^2 + 1) dx$.